The second midterm will test material covered in lectures 10 through 18.

Specific skills that may be tested include (the following list may not be exhaustive):

## 1. Divide and Conquer Paradigm

- 1.A. Solving recurrences characterizing the running time of divide and conquer algorithms.
- 1.B. Familiarity with specific Divide and Conquer Algorithms and the running times: Binary Search, Merge Sort, Quick Sort, Karatsuba's Algorithm, Linear Selection.
- 1.C. Ability to design and analyze divide and conquer algorithms for new problems.

### 2. Dynamic Programming Algorithms

- 2.A. Using the dynamic programming methodology to design algorithms for new problems.
- 2.B. Ability to analyze the running time of dynamic programming algorithms.

# 3. Graphs

- **3.A.** Basic definitions of undirected and directed graphs, DAGs, paths, cycles.
- **3.B.** Definitions of reachable nodes, connected components, and strongly connected components.
- **3.C.** Understand the structure of directed graphs in terms of the meta-graph of strongly connected components.
- **3.D.** Understand the structure of DAGs: sources, sinks and topological sort.
- **3.E.** Solving dynamic-programming problems using problems on DAGs.

## 4. Graph Search

- **4.A.** Understand properties of the basic search algorithm and its running time.
- **4.B.** Understand properties of **DFS** traversal on directed and undirected graph.
- **4.C.** Understand properties of the **DFS** tree.
- **4.D.** Algorithms based on search for finding connected components in undirected graphs, checking whether a graph is a DAG, topological sort for DAGs, knowledge of a linear-time algorithm to create the meta-graph, finding a cycle in a graph etc.
- **4.E.** Algorithms for DFAs/NFAs using graph algorithms.

#### 5. Shortest Paths in Graphs

- **5.A.** Understand properties of the **BFS** trees.
- **5.B.** Understand properties of **BFS** traversal on directed and undirected graph to find distances in unweighted graphs.
- **5.C.** Dijkstra's algorithm for finding single-source shortest paths in undirected and directed graphs with non-negative edge lengths.
- **5.D.** Negative length edges and Bellman-Ford algorithm to check for negative length cycles or find shortest paths if there is none.
- **5.E.** Floyd-Warshall algorithm.
- **5.F.** Single-source shortest paths in DAGs linear time algorithm for arbitrary edge lengths.
- **5.G.** Shortest path trees and their basic properties.
- **5.H.** Dynamic programming for shortest path problems in graphs.

#### 6. Graph reductions and tricks

- **6.A.** Modeling problems via graphs and solving them using graph structure, reachability and shortest path algorithms.
- **6.B.** Adding sources, sinks, splitting edges, nodes
- **6.C.** Creating layered graphs