

## Problem type 1:

$L_1, L_2, \dots$  are all regular languages representable by the DFAs  $M_1 = (Q_1, \Sigma, \delta_1, s_1, A_1)$ ,  $M_2 = (Q_2, \Sigma, \delta_2, s_2, A_2)$ , etc.

Give the *formal* description of the NFA ( $N'$ ) that describes the language below that is the composite of one or more of the above regular languages.

(See variants below)

We want to see the definition in terms of:  $Q' = \dots$ ,  $\delta' = \dots$ ,  $s' = \dots$ ,  $A' = \dots$ . Assume  $\Sigma = \{\mathbf{0}, \mathbf{1}\}$ .

a. **BYC**

$$L' = L_1 \cup L_2$$

b. **BYE**

$$L' = \overline{L_1}$$

c. **BYA**

$$L' = L_1 \cdot L_2$$

d. **BYH**

$$L' = L_1 \cup \{\varepsilon\}$$

(adding empty string to strings  $L_1$  regardless of if it is there (or not))

e. **BYD**

$$L' = \mathbf{0} \cdot L_1$$

Add a **0** before every string in  $L_1$

f. **BYF**

$$L' = L_1 \cup \{\mathbf{0}\}$$

(add the string "**0**" to strings in  $L_1$  regardless of if it is there (or not))

g. **BYB**

$$L' = L_1 \cdot \mathbf{0}$$

Add a **0** after every string in  $L_1$

h. **BYG**

$$L' = \{\mathbf{0}^* x \mathbf{0}^* a \mathbf{0}^* y \mathbf{0}^* \mid w = xay \in L_1, a \in \Sigma, x, y \in \Sigma^*\}$$

(basically what this is saying is that  $L'$  will accept any string in  $L_1$  and that string in  $L_1$  can have any number of **0**'s shoved in between each character).